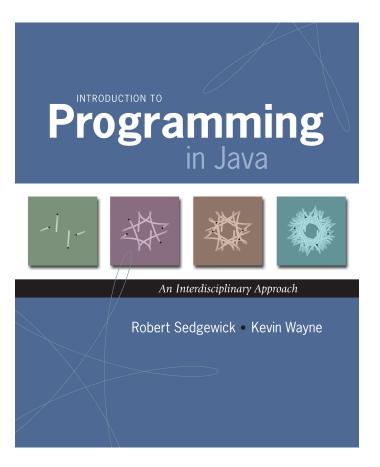
# 4.3 Stacks and Queues



#### Data Types and Data Structures

#### Data types.

- Set of values.
- Set of operations on those values.
- Some are built in to Java: int, double, char, ...
- Most are not: Complex, Picture, Stack, Queue, Graph, ...

this lecture

#### Data structures.

- Represent data or relationships among data.
- Some are built into Java: arrays, String,...
- Most are not: linked list, circular list, tree, sparse array, graph, ....



# Collections

#### Fundamental data types.

- Set of operations (add, remove, test if empty) on generic data.
- Intent is clear when we insert.
- Which item do we remove?

Stack. [LIFO = last in first out] ← this lecture

- Remove the item most recently added.
- Ex: cafeteria trays, Web surfing.

#### Queue. [FIFO = first in, first out]

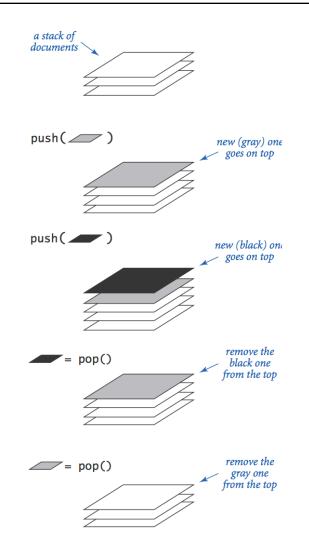
- Remove the item least recently added.
- Ex: Registrar's line.

#### Symbol table.

— next lecture

- Remove the item with a given key.
- Ex: Phone book.

# Stacks



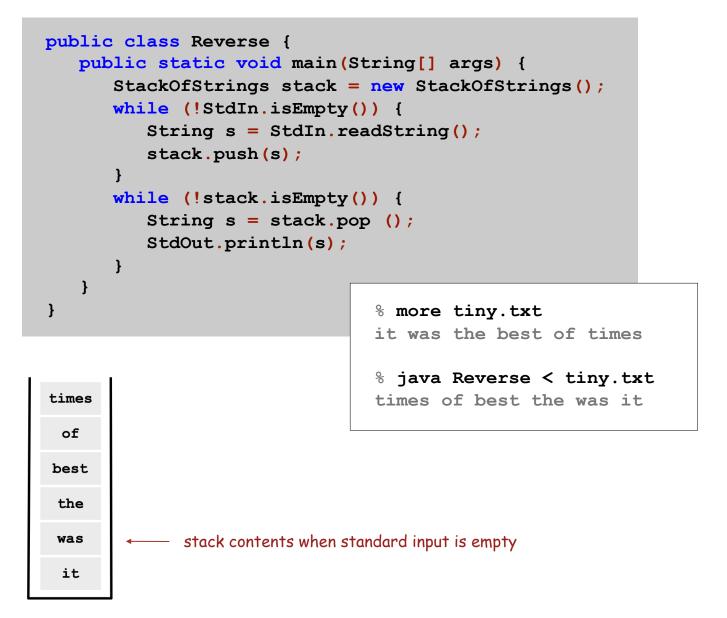
#### Stack API

# public class \*StackOfStrings \*StackOfStrings() create an empty stack boolean isEmpty() is the stack empty? void push(String item) push a string onto the stack String pop() pop the stack

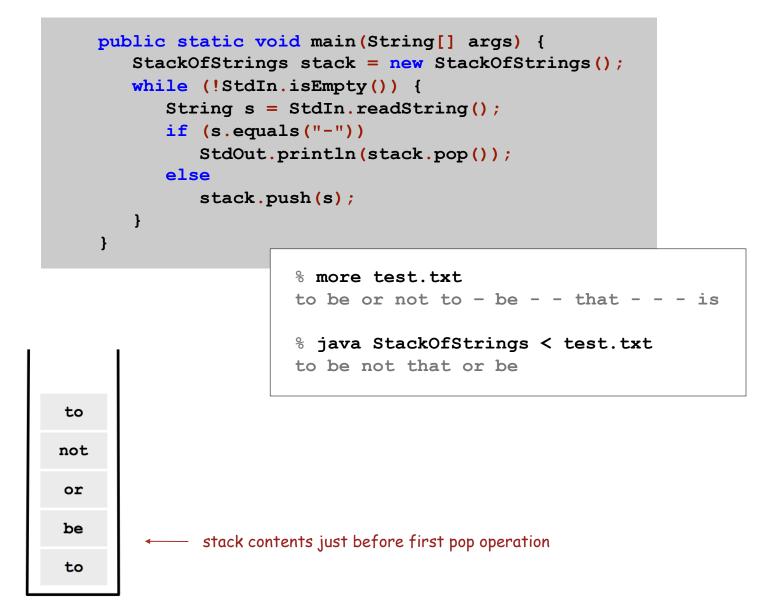


```
public class Reverse {
    public static void main(String[] args) {
        StackOfStrings stack = new StackOfStrings();
        while (!StdIn.isEmpty())
            stack.push(StdIn.readString());
        while (!stack.isEmpty())
            StdOut.println(stack.pop());
        }
}
```

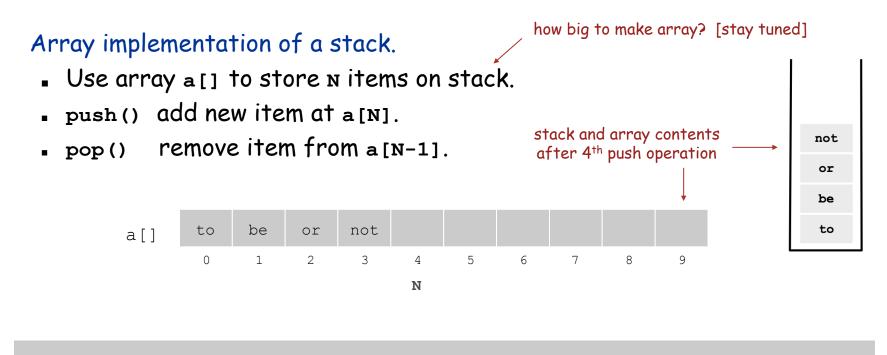
Stack Client Example 1: Reverse



Stack Client Example 2: Test Client



## Stack: Array Implementation



# Array Stack: Test Client Trace

|      | StdIn StdOut |      | N   |    | a[] |    |      |    |
|------|--------------|------|-----|----|-----|----|------|----|
|      |              |      | N - | 0  | 1   | 2  | 3    | 4  |
|      |              |      | 0   |    |     |    |      |    |
| push | to           |      | 1   | to |     |    |      |    |
|      | be           |      | 2   | to | be  |    |      |    |
|      | or           |      | 3   | to | be  | or |      |    |
|      | not          |      | 4   | to | be  | or | not  |    |
|      | to           |      | 5   | to | be  | or | not  | to |
| рор  | -            | to   | 4   | to | be  | or | not  | to |
|      | be           |      | 5   | to | be  | or | not  | be |
|      | -            | be   | 4   | to | be  | or | not  | be |
|      | -            | not  | 3   | to | be  | or | not  | be |
|      | that         |      | 4   | to | be  | or | that | be |
|      | _            | that | 3   | to | be  | or | that | be |
|      | _            | or   | 2   | to | be  | or | that | be |
|      | _            | be   | 1   | to | be  | or | that | be |
|      | is           |      | 2   | to | is  | or | not  | to |

## Array Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to client-supplied capacity, not number of items.

Problem.

- API does not call for capacity (bad to change API).
- Client might use multiple stacks.
- Client might not know what capacity to use.

Challenge. Stack implementation where size is not fixed ahead of time.

# Linked Lists

Sequential vs. Linked Allocation

Sequential allocation. Put object one after another.

- TOY: consecutive memory cells.
- Java: array of objects.

Linked allocation. Include in each object a link to the next one.

- TOY: link is memory address of next object.
- Java: link is reference to next object.

#### Key distinctions. get i<sup>th</sup> element

- Array: random access, fixed size.
- Linked list: sequential access, variable size.

aet next element

| addr | value   | addr | value   |    |
|------|---------|------|---------|----|
| C0   | "Alice" | C0   | "Carol" | •  |
| C1   | "Bob"   | C1   | null    |    |
| C2   | "Carol" | C2   | -       |    |
| С3   | -       | С3   | -       |    |
| C4   | -       | C4   | "Alice" |    |
| C5   | -       | C5   | CA      |    |
| C6   | -       | C6   | -       |    |
| C7   | -       | C7   | -       |    |
| C8   | -       | C8   | -       |    |
| С9   | -       | С9   | -       |    |
| CA   | -       | CA   | "Bob"   | ┥┙ |
| СВ   | -       | СВ   | C0      |    |

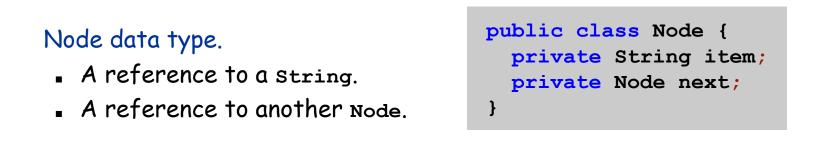
array

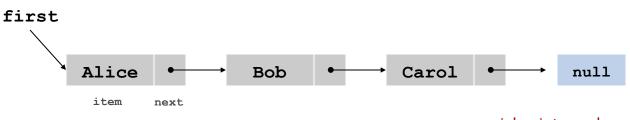
linked list

# Linked Lists

#### Linked list.

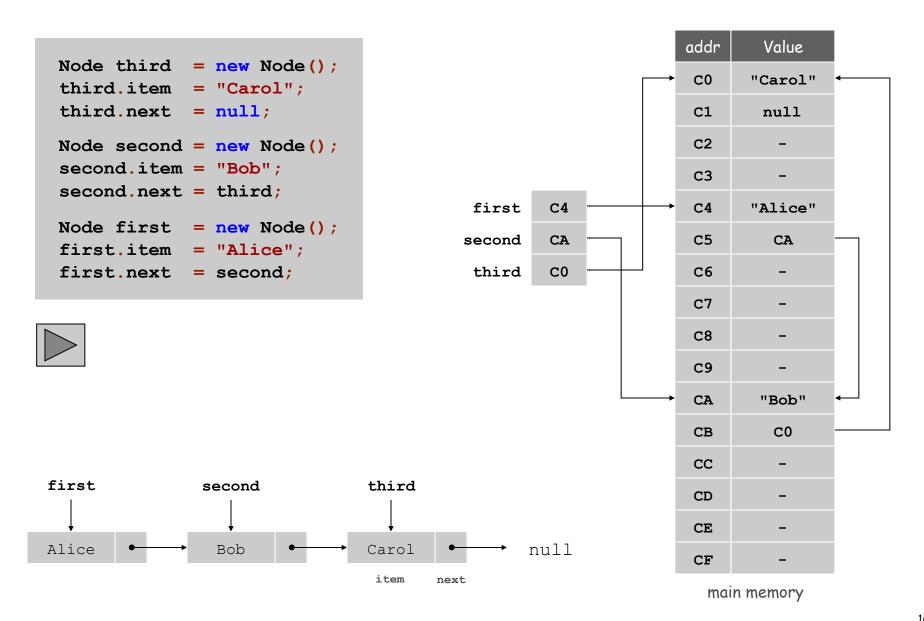
- A recursive data structure.
- An item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.



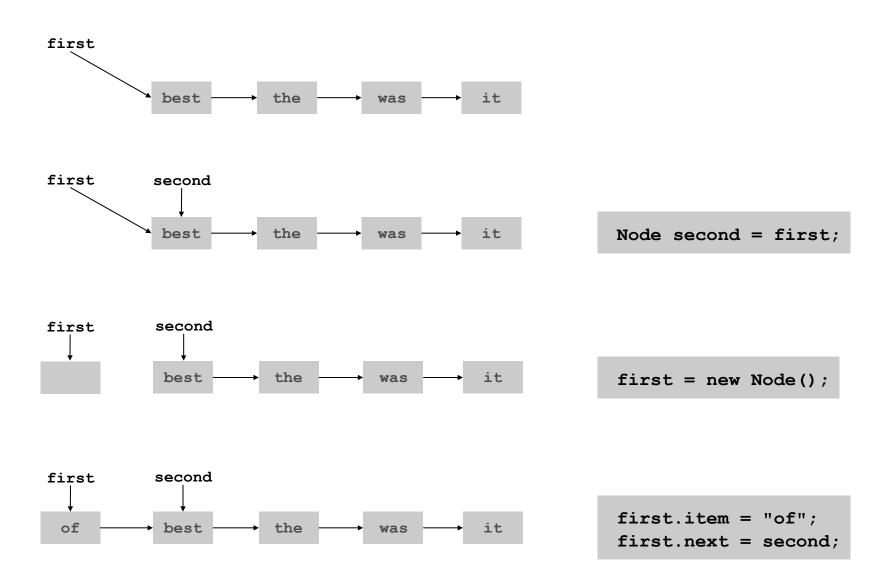


special pointer value null terminates list

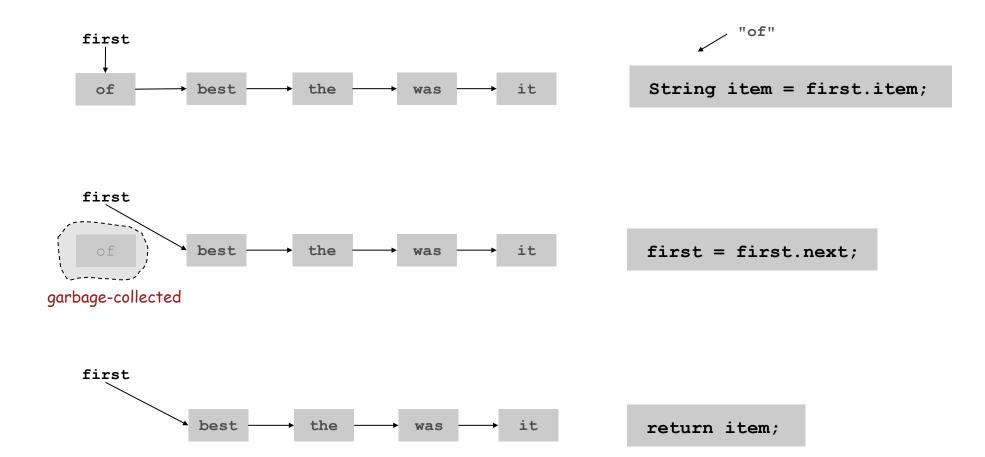
## Building a Linked List



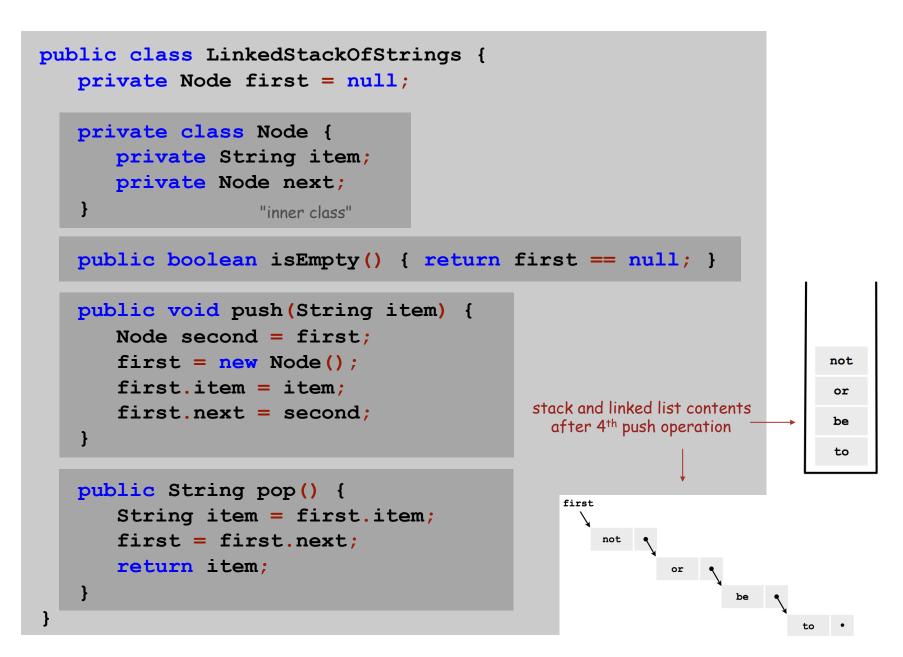
#### Stack Push: Linked List Implementation



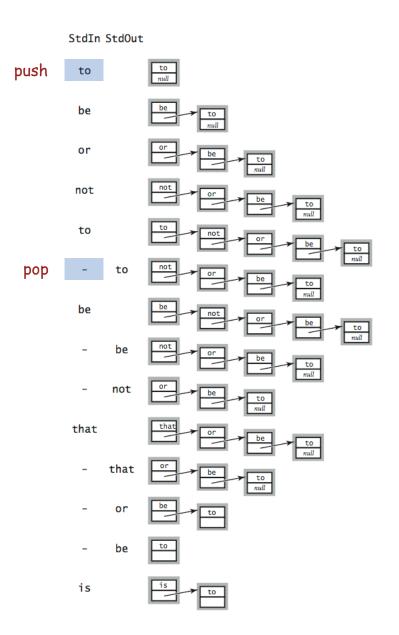
Stack Pop: Linked List Implementation



#### Stack: Linked List Implementation



#### Linked List Stack: Test Client Trace



Linked List Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to number of items in stack.

Stack Data Structures: Tradeoffs

Two data structures to implement Stack data type.

#### Array.

- Every push/pop operation take constant time.
- But... must fix maximum capacity of stack ahead of time.

#### Linked list.

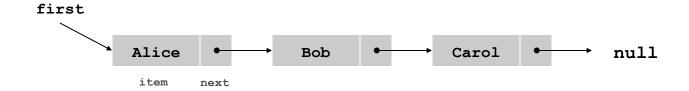
- Every push/pop operation takes constant time.
- But... uses extra space and time to deal with references.

List Processing Challenge 1

Q. What does the following code fragment do?

```
for (Node x = first; x != null; x = x.next) {
   StdOut.println(x.item);
}
```

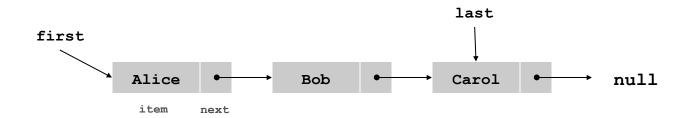




List Processing Challenge 2

Q. What does the following code fragment do?

```
Node last = new Node();
last.item = StdIn.readString();
last.next = null;
Node first = last;
while (!StdIn.isEmpty()) {
   last.next = new Node();
   last = last.next;
   last.item = StdIn.readString();
   last.next = null;
}
```



# Parameterized Data Types

#### Parameterized Data Types

We implemented: stackOfstrings.

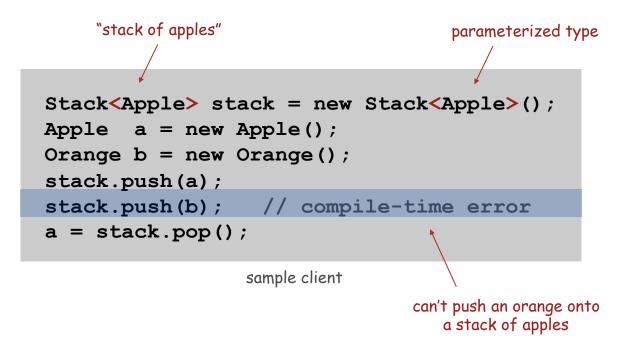
We also want: StackOfURLs, StackOfInts, ...

Strawman. Implement a separate stack class for each type.

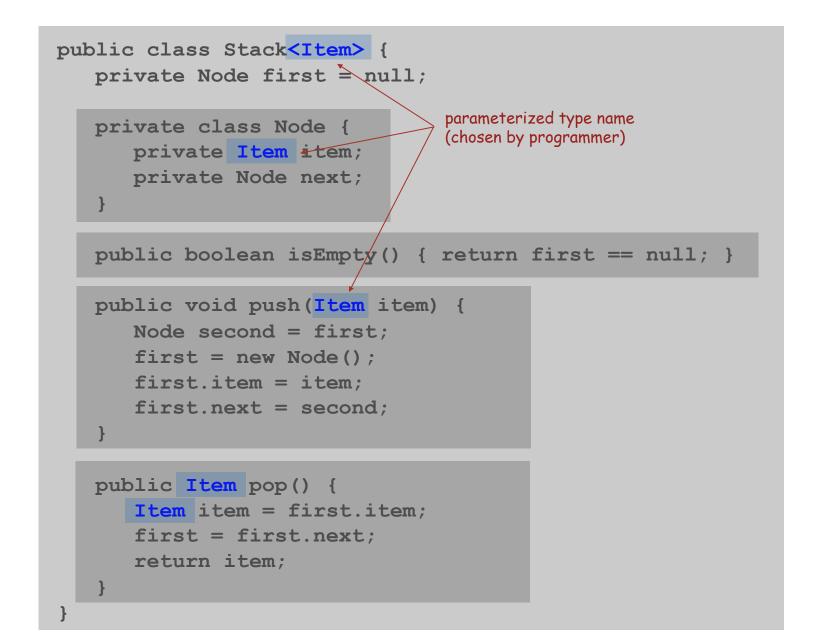
- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.

#### Generics

Generics. Parameterize stack by a single type.



#### Generic Stack: Linked List Implementation



### Autoboxing

Generic stack implementation. Only permits reference types.

#### Wrapper type.

- Each primitive type has a wrapper reference type.
- Ex: Integer is wrapper type for int.

Autoboxing. Automatic cast from primitive type to wrapper type. Autounboxing. Automatic cast from wrapper type to primitive type.

# Stack Applications

#### Real world applications.

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.

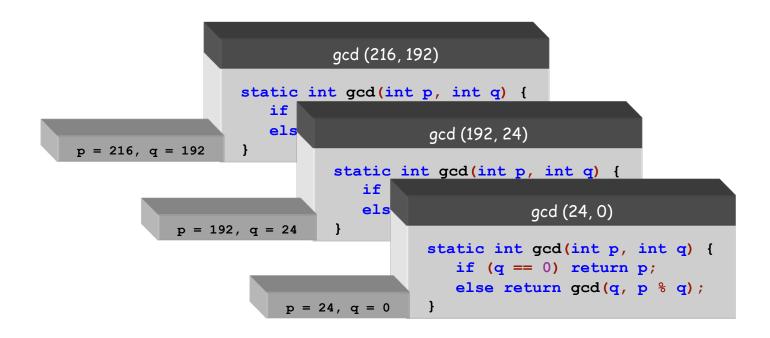
# Function Calls

How a compiler implements functions.

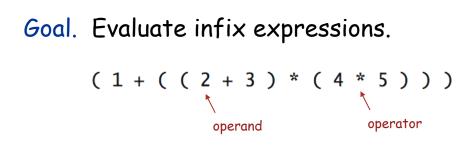
- Function call: push local environment and return address.
- Return: pop return address and local environment.

Recursive function. Function that calls itself.

Note. Can always use an explicit stack to remove recursion.



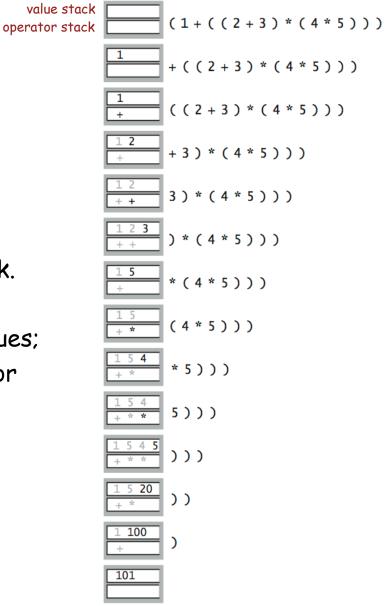
# Arithmetic Expression Evaluation



Two stack algorithm. [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the operand stack.

Context. An interpreter!



### Arithmetic Expression Evaluation

```
public class Evaluate {
   public static void main(String[] args) {
      Stack<String> ops = new Stack<String>();
      Stack<Double> vals = new Stack<Double>();
      while (!StdIn.isEmpty()) {
         String s = StdIn.readString();
                (s.equals("("))
         if
         else if (s.equals("+")) ops.push(s);
         else if (s.equals("*")) ops.push(s);
         else if (s.equals(")")) {
            String op = ops.pop();
                  (op.equals("+")) vals.push(vals.pop() + vals.pop());
            if
            else if (op.equals("*")) vals.push(vals.pop() * vals.pop());
         }
         else vals.push(Double.parseDouble(s));
      StdOut.println(vals.pop());
   }
}
                        % java Evaluate
                        (1 + ((2 + 3) * (4 * 5)))
                        101.0
```

#### Correctness

Why correct? When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

(1+((2+3)\*(4\*5)))

So it's as if the original input were:

(1+(5\*(4\*5)))

Repeating the argument:

( 1 + ( 5 \* 20 ) ) ( 1 + 100 ) 101

Extensions. More ops, precedence order, associativity, whitespace.

1 + (2 - 3 - 4) \* 5 \* sqrt(6\*6 + 7\*7)

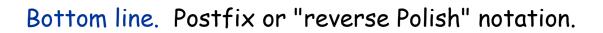
Stack-Based Programming Languages

Observation 1. Remarkably, the 2-stack algorithm computes the same value if the operator occurs after the two values.

(1((23+)(45\*)\*)+)

Observation 2. All of the parentheses are redundant!

1 2 3 + 4 5 \* \* +

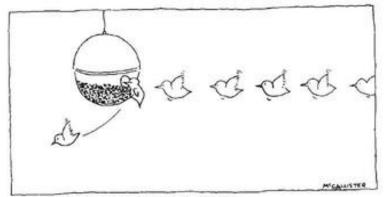


Applications. Postscript, Forth, calculators, Java virtual machine, ...



Jan Lukasiewicz

# Queues

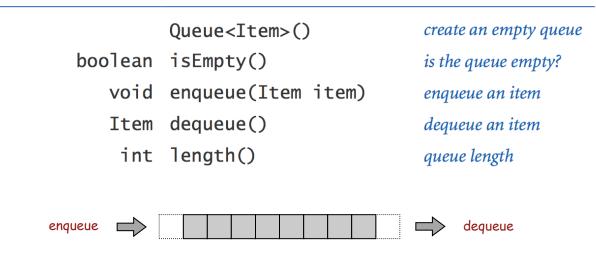


Drawing by McCallister, @ 1977 The New Yorker Magazine, Inc.



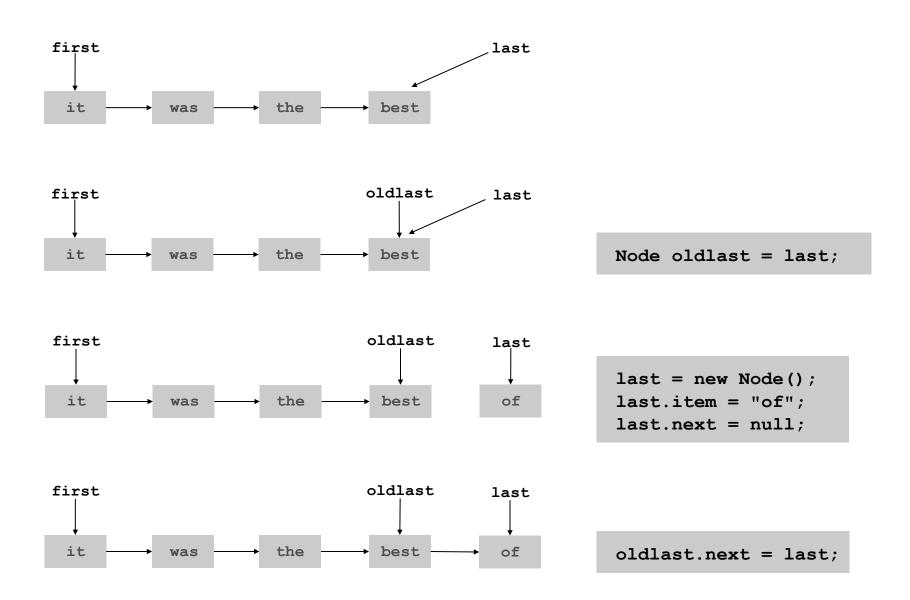
#### Queue API

public class Queue<Item>

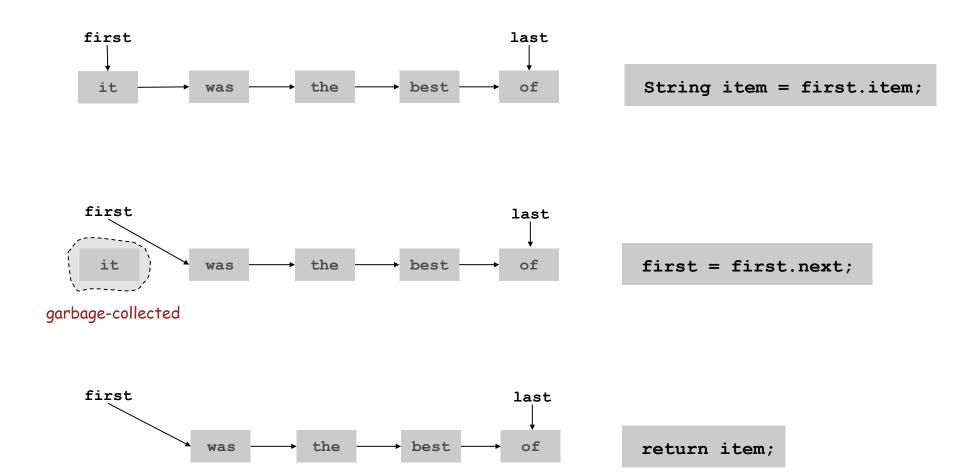


```
public static void main(String[] args) {
    Queue<String> q = new Queue<String>();
    q.enqueue("Vertigo");
    q.enqueue("Just Lose It");
    q.enqueue("Pieces of Me");
    q.enqueue("Pieces of Me");
    while(!q.isEmpty())
        StdOut.println(q.dequeue());
}
```

Enqueue: Linked List Implementation



### Dequeue: Linked List Implementation



#### Queue: Linked List Implementation

```
public class Queue<Item> {
  private Node first, last;
  private class Node { Item item; Node next; }
  public boolean isEmpty() { return first == null; }
   public void enqueue(Item item) {
     Node oldlast = last;
      last = new Node();
      last.item = item;
      last.next = null;
      if (isEmpty()) first = last;
              oldlast.next = last;
      else
  public Item dequeue() {
      Item item = first.item;
      first = first.next;
      if (isEmpty()) last = null;
      return item;
   }
```

# Queue Applications

## Some applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

## Simulations of the real world.

- Guitar string.
- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

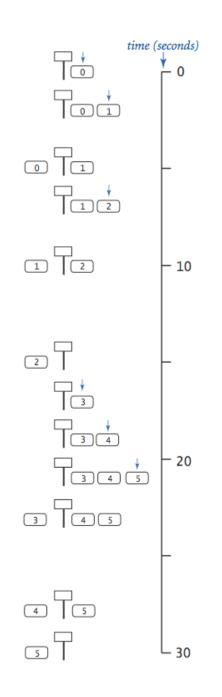
## M/D/1 Queuing Model

#### M/D/1 queue.

- Customers are serviced at fixed rate of  $\mu$  per minute.
- Customers arrive according to Poisson process at rate of  $\lambda$  per minute.

 $Pr[X \le x] = 1 - e^{-\lambda x}$  Arrival rate  $\lambda \longrightarrow Departure rate \mu$  Infinite queue Server

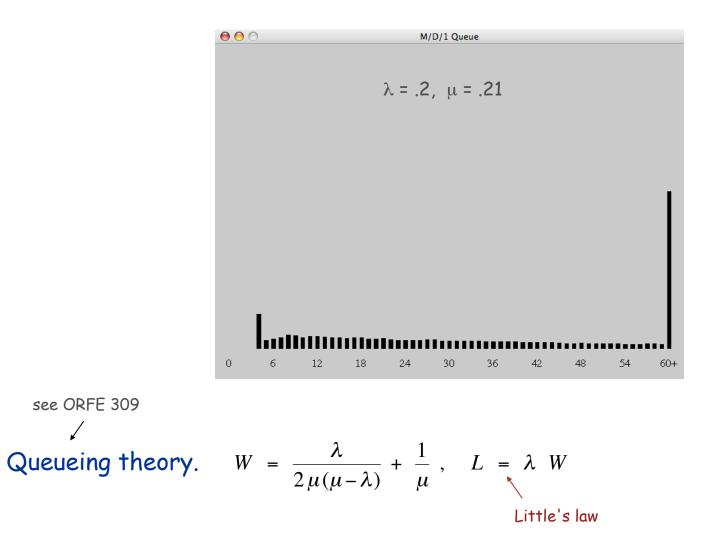
- Q. What is average wait time W of a customer?
- Q. What is average number of customers L in system?



|   | arrival | departure | wait |
|---|---------|-----------|------|
| 0 | 0       | 5         | 5    |
| 1 | 2       | 10        | 8    |
| 2 | 7       | 15        | 8    |
| 3 | 17      | 23        | 6    |
| 4 | 19      | 28        | 9    |
| 5 | 21      | 30        | 9    |

```
public class MD1Queue {
   public static void main(String[] args) {
      double lambda = Double.parseDouble(args[0]);
                    = Double.parseDouble(args[1]);
      double mu
      Queue<Double> q = new Queue<Double>();
      double nextArrival = StdRandom.exp(lambda);
      double nextService = nextArrival + 1/mu;
      while(true) {
         if (nextArrival < nextService) {</pre>
                                                            arrival
            q.enqueue(nextArrival);
            nextArrival += StdRandom.exp(lambda);
         }
         else {
                                                            service
            double wait = nextService - q.dequeue();
            // add waiting time to histogram
            if (q.isEmpty()) nextService = nextArrival + 1/mu;
                             nextService = nextService + 1/mu;
            else
}
```

Observation. As service rate approaches arrival rate, service goes to h\*\*\*.



# Summary

#### Stacks and queues are fundamental ADTs.

- Array implementation.
- Linked list implementation.
- Different performance characteristics.

### Many applications.