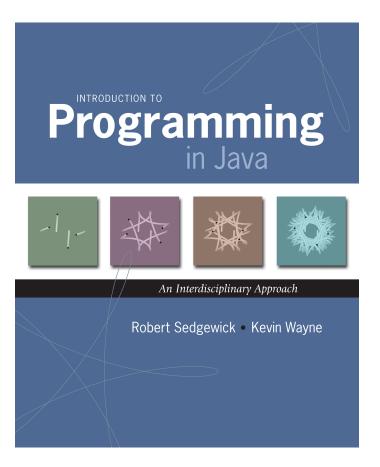
4.3 Stacks and Queues



Data Types and Data Structures

Data types.

- Set of values.
- Set of operations on those values.
- Some are built in to Java: int, double, char, ...
- Most are not: Complex, Picture, Stack, Queue, Graph, ...

this lecture

Data structures.

- Represent data or relationships among data.
- Some are built into Java: arrays, String,...
- Most are not: linked list, circular list, tree, sparse array, graph,



Collections

Fundamental data types.

- Set of operations (add, remove, test if empty) on generic data.
- Intent is clear when we insert.
- Which item do we remove?

Stack. [LIFO = last in first out] ← this lecture

- Remove the item most recently added.
- Ex: cafeteria trays, Web surfing.

Queue. [FIFO = first in, first out]

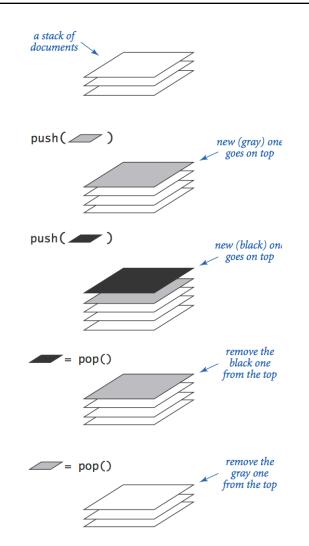
- Remove the item least recently added.
- Ex: Registrar's line.

Symbol table.

— next lecture

- Remove the item with a given key.
- Ex: Phone book.

Stacks



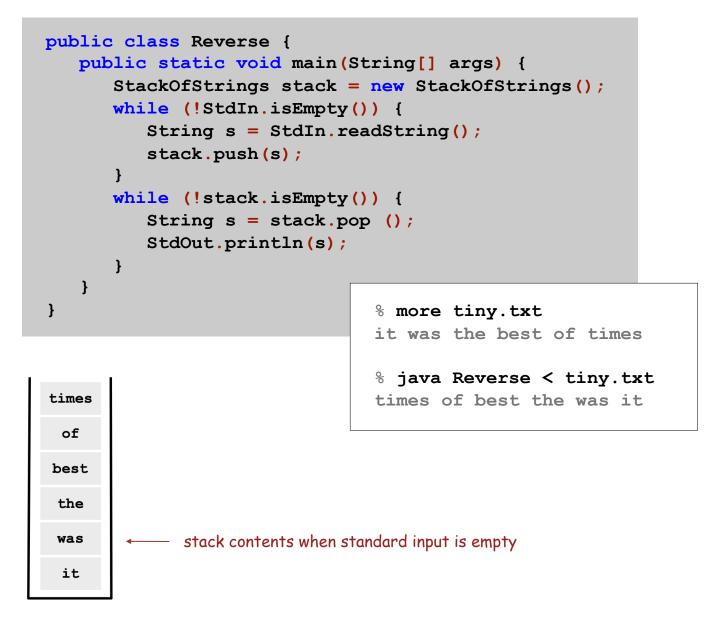
Stack API

public class *StackOfStrings *StackOfStrings() create an empty stack boolean isEmpty() is the stack empty? void push(String item) push a string onto the stack String pop() pop the stack

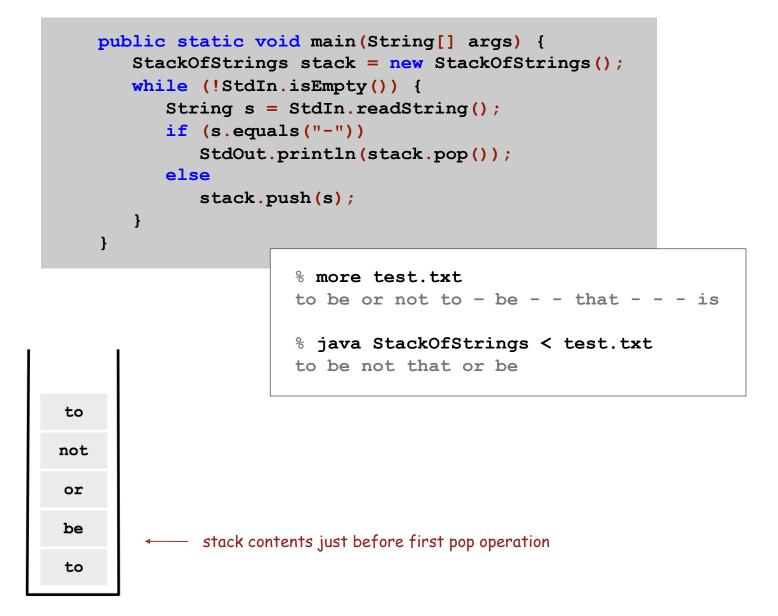


```
public class Reverse {
    public static void main(String[] args) {
        StackOfStrings stack = new StackOfStrings();
        while (!StdIn.isEmpty())
            stack.push(StdIn.readString());
        while (!stack.isEmpty())
            StdOut.println(stack.pop());
        }
}
```

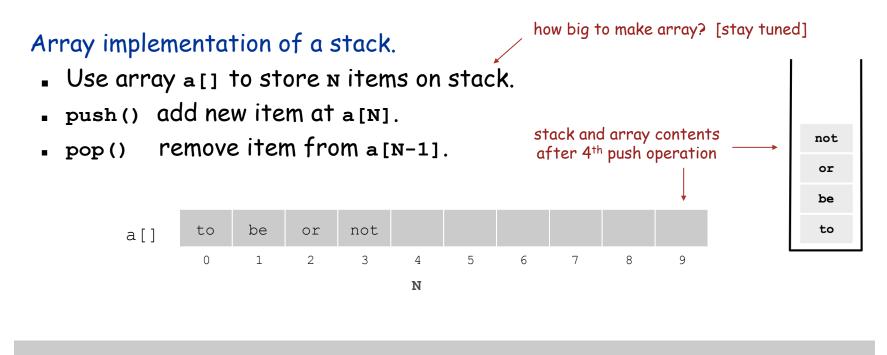
Stack Client Example 1: Reverse



Stack Client Example 2: Test Client



Stack: Array Implementation



Array Stack: Test Client Trace

	StdIn StdOut		N		a[]			
			N -	0	1	2	3	4
			0					
push	to		1	to				
	be		2	to	be			
	or		3	to	be	or		
	not		4	to	be	or	not	
	to		5	to	be	or	not	to
рор	-	to	4	to	be	or	not	to
	be		5	to	be	or	not	be
	-	be	4	to	be	or	not	be
	-	not	3	to	be	or	not	be
	that		4	to	be	or	that	be
	_	that	3	to	be	or	that	be
	_	or	2	to	be	or	that	be
	_	be	1	to	be	or	that	be
	is		2	to	is	or	not	to

Array Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to client-supplied capacity, not number of items.

Problem.

- API does not call for capacity (bad to change API).
- Client might use multiple stacks.
- Client might not know what capacity to use.

Challenge. Stack implementation where size is not fixed ahead of time.

Linked Lists

Sequential vs. Linked Allocation

Sequential allocation. Put object one after another.

- TOY: consecutive memory cells.
- Java: array of objects.

Linked allocation. Include in each object a link to the next one.

- TOY: link is memory address of next object.
- Java: link is reference to next object.

Key distinctions. get ith element

- Array: random access, fixed size.
- Linked list: sequential access, variable size.

aet next element

addr	value	addr	value	
C0	"Alice"	C0	"Carol"	•
C1	"Bob"	C1	null	
C2	"Carol"	C2	-	
С3	-	С3	-	
C4	-	C4	"Alice"	
C5	-	C5	CA	
C6	-	C6	-	
C7	-	C7	-	
C8	-	C8	-	
С9	-	С9	-	
CA	-	CA	"Bob"	┥┙
СВ	-	СВ	C0	

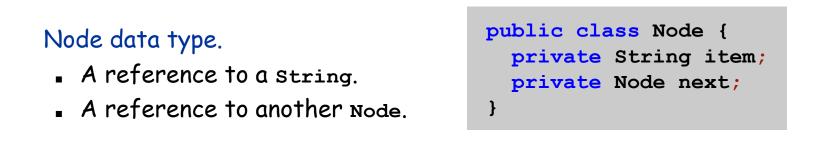
array

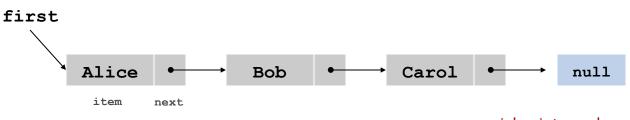
linked list

Linked Lists

Linked list.

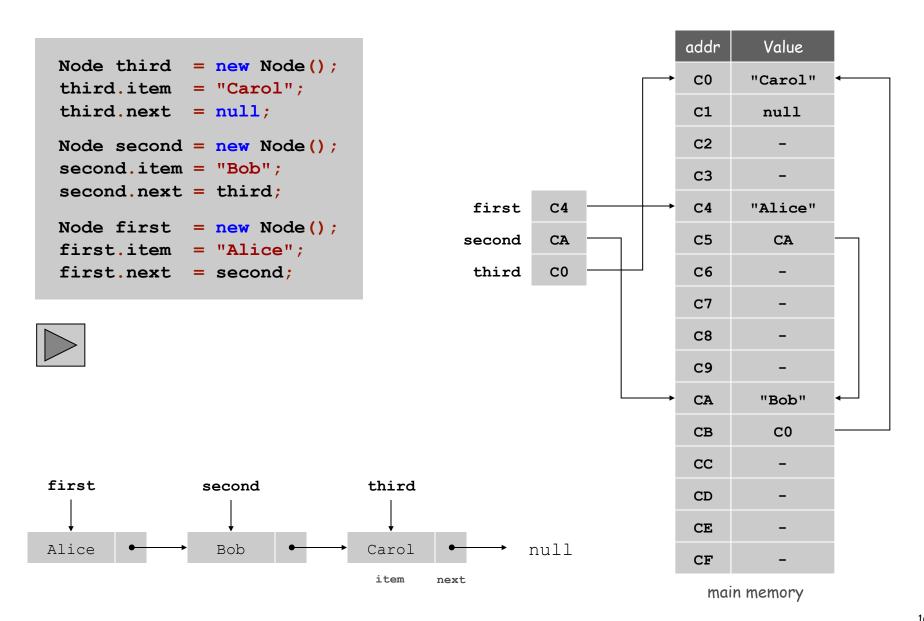
- A recursive data structure.
- An item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.



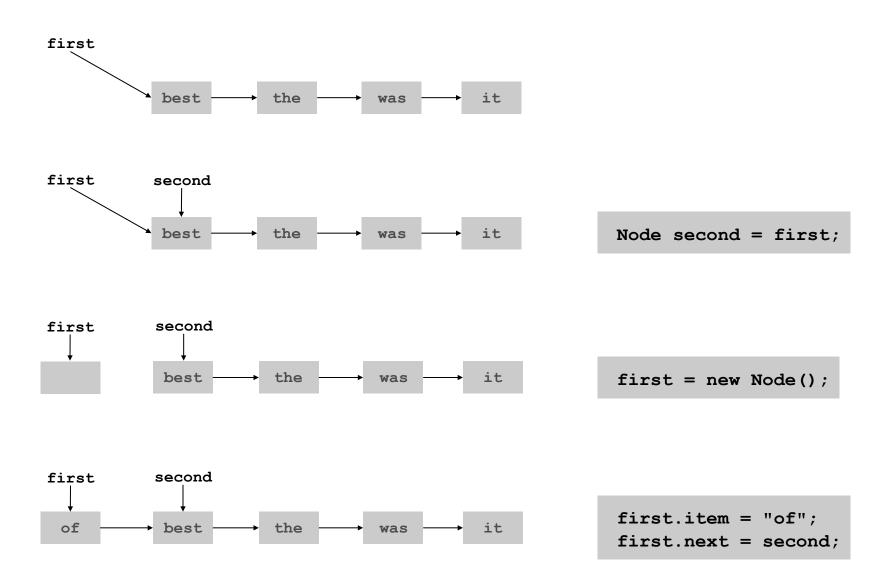


special pointer value null terminates list

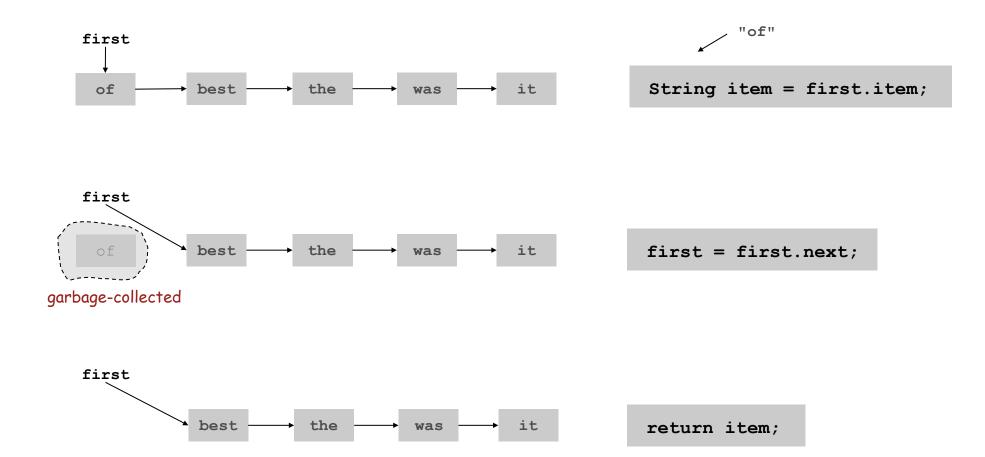
Building a Linked List



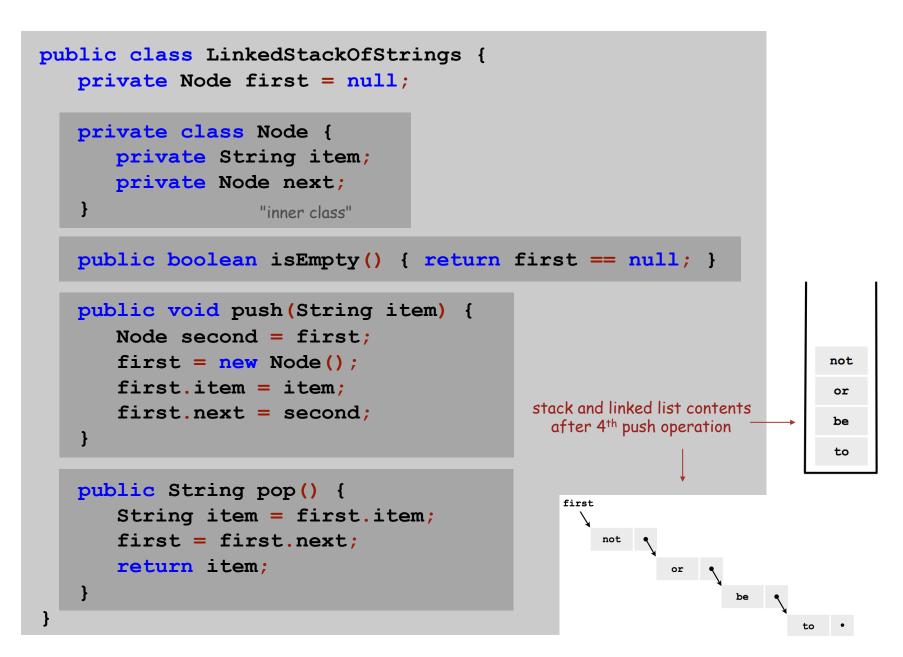
Stack Push: Linked List Implementation



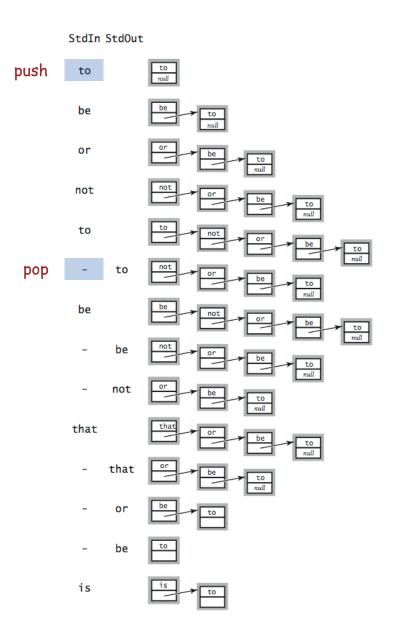
Stack Pop: Linked List Implementation



Stack: Linked List Implementation



Linked List Stack: Test Client Trace



Linked List Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to number of items in stack.

Stack Data Structures: Tradeoffs

Two data structures to implement Stack data type.

Array.

- Every push/pop operation take constant time.
- But... must fix maximum capacity of stack ahead of time.

Linked list.

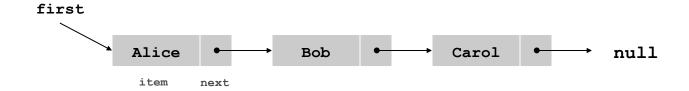
- Every push/pop operation takes constant time.
- But... uses extra space and time to deal with references.

List Processing Challenge 1

Q. What does the following code fragment do?

```
for (Node x = first; x != null; x = x.next) {
   StdOut.println(x.item);
}
```

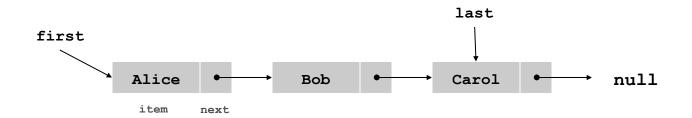




List Processing Challenge 2

Q. What does the following code fragment do?

```
Node last = new Node();
last.item = StdIn.readString();
last.next = null;
Node first = last;
while (!StdIn.isEmpty()) {
   last.next = new Node();
   last = last.next;
   last.item = StdIn.readString();
   last.next = null;
}
```



Parameterized Data Types

Parameterized Data Types

We implemented: stackOfstrings.

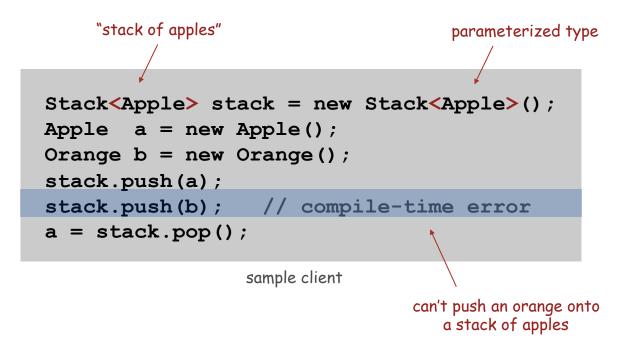
We also want: StackOfURLs, StackOfInts, ...

Strawman. Implement a separate stack class for each type.

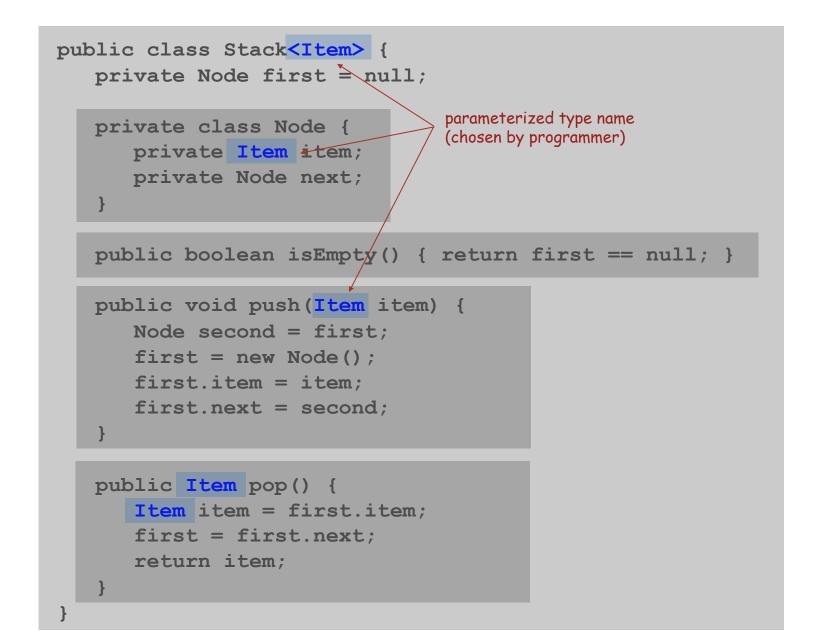
- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.

Generics

Generics. Parameterize stack by a single type.



Generic Stack: Linked List Implementation



Autoboxing

Generic stack implementation. Only permits reference types.

Wrapper type.

- Each primitive type has a wrapper reference type.
- Ex: Integer is wrapper type for int.

Autoboxing. Automatic cast from primitive type to wrapper type. Autounboxing. Automatic cast from wrapper type to primitive type.

Stack Applications

Real world applications.

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.

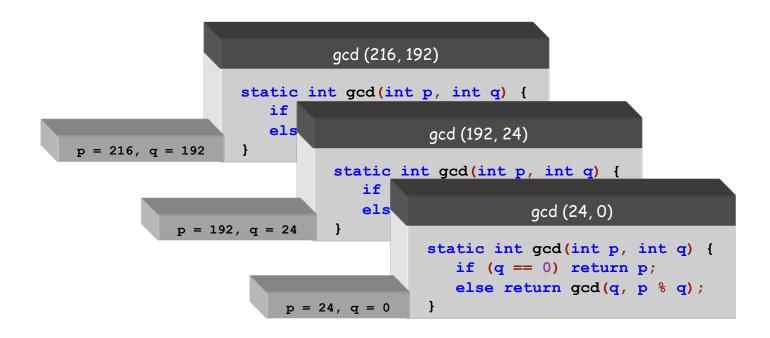
Function Calls

How a compiler implements functions.

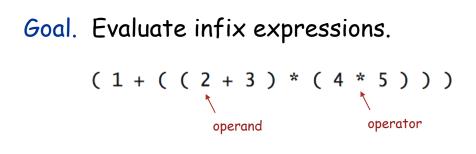
- Function call: push local environment and return address.
- Return: pop return address and local environment.

Recursive function. Function that calls itself.

Note. Can always use an explicit stack to remove recursion.



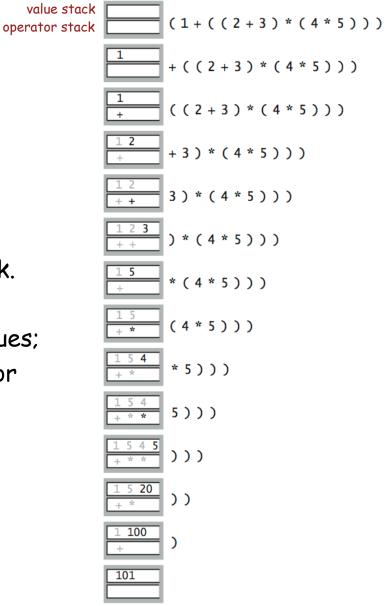
Arithmetic Expression Evaluation



Two stack algorithm. [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the operand stack.

Context. An interpreter!



Arithmetic Expression Evaluation

```
public class Evaluate {
   public static void main(String[] args) {
      Stack<String> ops = new Stack<String>();
      Stack<Double> vals = new Stack<Double>();
      while (!StdIn.isEmpty()) {
         String s = StdIn.readString();
                (s.equals("("))
         if
         else if (s.equals("+")) ops.push(s);
         else if (s.equals("*")) ops.push(s);
         else if (s.equals(")")) {
            String op = ops.pop();
                  (op.equals("+")) vals.push(vals.pop() + vals.pop());
            if
            else if (op.equals("*")) vals.push(vals.pop() * vals.pop());
         }
         else vals.push(Double.parseDouble(s));
      StdOut.println(vals.pop());
   }
}
                        % java Evaluate
                        (1 + ((2 + 3) * (4 * 5)))
                        101.0
```

Correctness

Why correct? When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

(1+((2+3)*(4*5)))

So it's as if the original input were:

(1+(5*(4*5)))

Repeating the argument:

(1 + (5 * 20)) (1 + 100) 101

Extensions. More ops, precedence order, associativity, whitespace.

1 + (2 - 3 - 4) * 5 * sqrt(6*6 + 7*7)

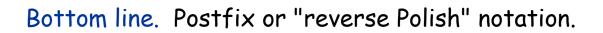
Stack-Based Programming Languages

Observation 1. Remarkably, the 2-stack algorithm computes the same value if the operator occurs after the two values.

(1((23+)(45*)*)+)

Observation 2. All of the parentheses are redundant!

1 2 3 + 4 5 * * +

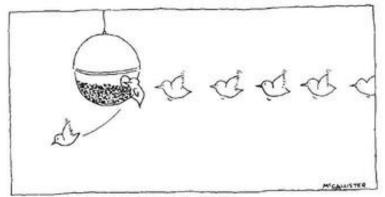


Applications. Postscript, Forth, calculators, Java virtual machine, ...



Jan Lukasiewicz

Queues

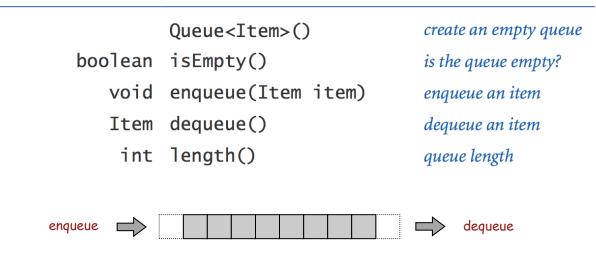


Drawing by McCallister, @ 1977 The New Yorker Magazine, Inc.



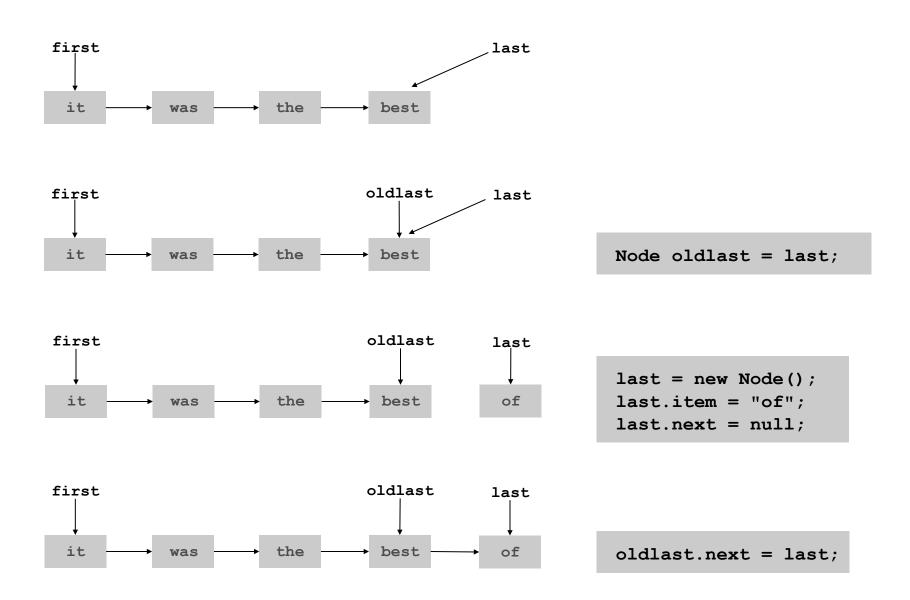
Queue API

public class Queue<Item>

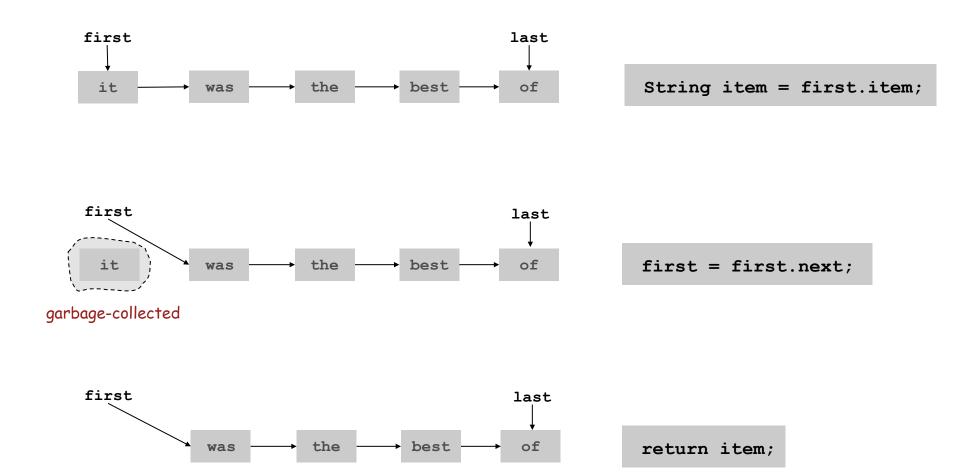


```
public static void main(String[] args) {
    Queue<String> q = new Queue<String>();
    q.enqueue("Vertigo");
    q.enqueue("Just Lose It");
    q.enqueue("Pieces of Me");
    q.enqueue("Pieces of Me");
    while(!q.isEmpty())
        StdOut.println(q.dequeue());
}
```

Enqueue: Linked List Implementation



Dequeue: Linked List Implementation



Queue: Linked List Implementation

```
public class Queue<Item> {
  private Node first, last;
  private class Node { Item item; Node next; }
  public boolean isEmpty() { return first == null; }
   public void enqueue(Item item) {
     Node oldlast = last;
      last = new Node();
      last.item = item;
      last.next = null;
      if (isEmpty()) first = last;
              oldlast.next = last;
      else
  public Item dequeue() {
      Item item = first.item;
      first = first.next;
      if (isEmpty()) last = null;
      return item;
   }
```

Queue Applications

Some applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

Simulations of the real world.

- Guitar string.
- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

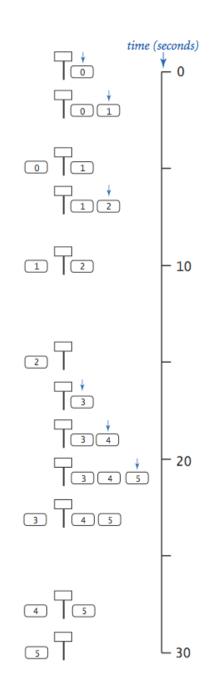
M/D/1 Queuing Model

M/D/1 queue.

- Customers are serviced at fixed rate of μ per minute.
- Customers arrive according to Poisson process at rate of λ per minute.

 $Pr[X \le x] = 1 - e^{-\lambda x}$ Arrival rate $\lambda \longrightarrow Departure rate \mu$ Infinite queue Server

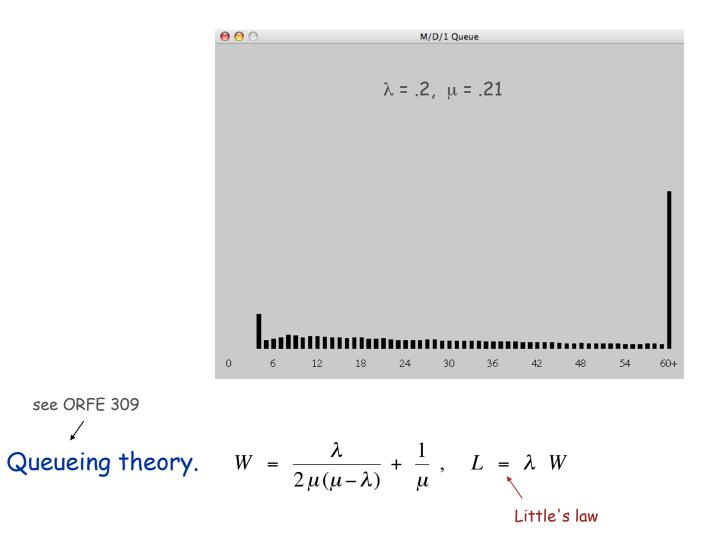
- Q. What is average wait time W of a customer?
- Q. What is average number of customers L in system?



	arrival	departure	wait
0	0	5	5
1	2	10	8
2	7	15	8
3	17	23	6
4	19	28	9
5	21	30	9

```
public class MD1Queue {
   public static void main(String[] args) {
      double lambda = Double.parseDouble(args[0]);
                    = Double.parseDouble(args[1]);
      double mu
      Queue<Double> q = new Queue<Double>();
      double nextArrival = StdRandom.exp(lambda);
      double nextService = nextArrival + 1/mu;
      while(true) {
         if (nextArrival < nextService) {</pre>
                                                            arrival
            q.enqueue(nextArrival);
            nextArrival += StdRandom.exp(lambda);
         }
         else {
                                                            service
            double wait = nextService - q.dequeue();
            // add waiting time to histogram
            if (q.isEmpty()) nextService = nextArrival + 1/mu;
                             nextService = nextService + 1/mu;
            else
}
```

Observation. As service rate approaches arrival rate, service goes to h***.



Summary

Stacks and queues are fundamental ADTs.

- Array implementation.
- Linked list implementation.
- Different performance characteristics.

Many applications.